DISTRIBUTION CHARACTERISTICS OF FERRO-TITANIUM OXIDE MINERAL ON LOW-GRADE IRON SAND

KARAKTERISTIK DISTRIBUSI MINERAL BESI-TITANIUM OKSIDA PADA PASIR BESI KADAR RENDAH

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ABSTRACT

Iron sand is known as one of the sources of TiO_2 in the form of ilmenite or titanomagnetite mineral. Irontitanium oxide mineral contained in Indonesia iron sand are classified as titanomagnetite. Indonesia possesses a lot of iron sand deposits such as at southern coast of Cilacap, Kebumen and other areas. The iron sand consists of magnetic and non-magnetic minerals as either loses or bound materials. Fractionation of Cilacap iron sand which employed three types of sieve (40, 60 and 80 meshes) showed that the iron sand is dominant in -40+60 fraction (68.38 g) while the most amount of iron and titania contents occurred at fraction of -80 mesh, namely 11.62 and 1.46%. Magnetic separation showed that the finer the particles and the higher the magnetic intensity, the higher the derived iron and titania. The process has also successfully increased the TiO_2 content more than 5 times, from 0.325 to 1.67%.

Keywords: iron sand, particle size, magnetic separation, titanium oxide.

ABSTRAK

Pasir besi dikenal sebagai salah satu sumber TiO₂ baik dalam bentuk mineral ilmenite atau titanomagnetite. Mineral Oksida besi-titanium yang terkandung dalam pasir besi Indonesia diklasifikasikan sebagai titanomagnetit. Indonesia mempunyai potensi pasir besi cukup banyak seperti di pantai selatan Cilacap, Kebumen dan daerah lainnya. Dalam pasir besi tersebut terkandung mineral magnetik dan bukan magnetik baik yang bersifat lepas maupun berasosiasi dengan mineral lain. Fraksinasi pasir besi Cilacap dengan tiga jenis ayakan (40, 60 dan 80 mesh) menunjukkan bahwa pasir besi dominan pada fraksi -40+60 mesh (68,38 gram) sedangkan kandungan besi dan TiO₂ terbanyak ada pada fraksi lolos 80 mesh, yaitu masing-masing 11,62 dan 1,46%. Separasi secara magnetik menunjukkan bahwa semakin halus ukuran partikel dan semakin tinggi intensitas magnetik yang digunakan semakin tinggi kadar besi dan titanium oksida yang diperoleh. Proses ini telah berhasil meningkatkan kandungan TiO₂, lebih dari lima kali lipat, yaitu dari 0,325% menjadi 1,67%.

Kata kunci: pasir besi, ukuran partikel, pemisahan magnetik, titanium oksida.

INTRODUCTION

Titanium dioxide (TiO_2) , also known as titanium (IV) oxide or titania, is a metal oxide that has a wide range of applications, from paint to sunscreen to food coloring due to its excellent characters such as white massive

crystal, non-toxic and environmental friendly as well as insoluble in water (Justicia *et al.*, 2002; Beer *et al.*, 2015; Shaheed and Hussein, 2015; Sprong *et al.*, 2015). The oxide is also used for making titanium metal. Such a metal is widely employed for making fighter aircraft, gas and chemical instruments, sports equipment, bike frame, jewelry, automotive, and medical equipment. The most important and strategic application of pure titanium and its alloy is in the airframe and aircraft engine industries (Barlow, 2015; Bedinger, 2015; Adams, 2016; Whitfield *et al.*, 2016). The titanium is alloyed with other metals such as aluminum, chrome, zirconium, etc.

The need of TiO₂ for the global market is predicted 4 - 7% through 2019, each year. Such a consumption notably goes to pigment industries and as the feed for titanium making. It is assumed that in 2025, the demand of total TiO₂ is up to 10.8 million ton. In 2015, the total demand of TiO₂ was reported up to 7.055 million tons. It was assumed that the increase of the total TiO₂ demand reached 5% a year. The deficit of such a material will occur in 2017 as the global production for TiO₂ is predicted up to 7.5 million tons and no significant increase of TiO₂ production through 2017 (Barlow, 2015; Bedinger, 2015; Adams, 2016; Whitfield et al., 2016).

The main feedstocks for production of titanium dioxide pigment currently used by commercial processes in the form of titania slag (high TiO₂ slag. The most common method for producing titania slag is smelting process which reduces iron oxides to liquid iron in large electric arc furnaces with raw material from ilmenite ore. The main product of smelting is titania slag containing approximately 75 to 85% TiO₂ (Middlemas, Fang and Fan, 2013; Gázquez *et al.*, 2014).

Few TiO₂-bearing minerals that are commercially used include ilmenite (FeTiO₃), leucoxene (Fe₂TiO₅), rutile (TiO₂), ulvöspinel (Fe₂TiO₄) and iron sand (Premaratne and Rowson, 2004; Babu, Vasumathi and Rao, 2009; Arndt, Kesler and Ganino, 2015). The iron sand is actually the beach sand that serves as the source of iron oxide and titanium oxide. Such the beach sands came from metamorphic and igneous rocks. There are two kinds of beach sand in nature, namely titanohematite and titanomagnetite. The former belongs to a mixture of ilmenite (FeTiO₃) and hematite (Fe₂O₃) while the later contains ulvöspinel or ulvite (Fe2TiO4) and magnetite (Fe₃O₄). Indonesia possesses titanium resources that come from the iron sand. Its type belongs to titan magnetite with

various TiO₂ content. TiO₂ levels generally found in deposits of titanomagnetite iron sand with levels ranging between 0,5-15% TiO₂ (Tampubolon, 2013). Currently, Indonesian iron sand is only used as a mixture of Portland cement. The material is not optimally used as a potential commodity of metal although the technoloav mineral for processing the Indonesian titanomagnetite has been found. Such a technology, namely pyrometallurgy, processes the sand into titania slag. However; the sand should be concentrated prior to processing it as the feed to obtain titania (Zhang, Zhu and Cheng, 2011).

The success of iron sand concentration depends on iron sand characteristics. Ansori (2013) who processed the iron sand from the southern coast of Kebumen Regency by a magnetic separator obtained the recovery of 66.46 % by weight with Fe total of 56.57 %. Condition used by Ansori (2013) was 200 Gauss of magnetic intensity and -120+120 mesh of particle size. The iron sand used in this study came from the southern coast of Cilacap and had been characterized its mineralogy, chemical and concentration. The magnetic separator was used in terms of concentrating the material. Parameters used for magnetic separator were particle size distribution and magnetic intensities of iron and titanium-containing sands. The purpose of all characterization study was determining the right concentration process for obtaining optimum TiO₂ concentrates.

METHODOLOGY

Samples used for this research came from Cilacap coastal which were prepared prior to mineral characteristic analyses and processing trial to get the concentrates. Figure 1 illustrated sample preparation of Cilacap iron beach sand for the research.

A series of preparation included washing, sampling and magnetic separation. The purpose of washing was to get rid of fine components such as clay while sampling contained quartering and splitting to get the representative samples. Magnetic separation was conducted using magnetic intensities of 1000, 2000 and 4000 Gausses. All preparation processes were shown in Figure 2.



Figure 1. A flow chart of iron sand preparation



Figure 2. A flow chart for magnetic separation

RESULTS AND DISCUSSION

Sieve analysis of the 12,626 kg-samples distributed the materials into four size fractions, namely +40, -40+60, -60+80 and -80 meshes as shown in Table 1. Of the four sieve equipment, sieve -40+60 mesh maintained the highest weight percentage

for all sieved samples. Each fraction was analyzed its total iron as well as its titanium dioxide contents. The result was presented in Table 2.

Titanium is actually an impurity element within the iron sand. The element needs to be physically separated in order to conventionally processing the sand by pyrometallurgy method. Yet the interlocking character between the iron and the titanium is a problem. The physical method cannot separate both materials (Sunaryo and 2010; Sufiandi, Sugihartono, 2011). Magnetic separation was conducted into 3 stages based on the employed magnetic intensities during the process. Such intensities included 1000, 2000 and 4000 Gausses. Of the four fractions. -80 mesh fraction was not processed. Chemical analyses were conducted to magnetic separation products to evaluate the total iron components and titanium oxide within the fractions. Table 3 illustrated such

compositions. Magnetic separation products were also assessed its mineralogical composition using XRD method. However, the tested samples were a little bit different from those for chemical analyses.

Analyzing the dominant mineral within the product of magnetic separation was conducted using XRD method. The analyzed samples included an original sample of -80 mesh, magnetic product of 1.00 g size -40+60 and -60+80 meshes as well as non-magnetic product size -40+60 mesh. Figure 3 through 6 showed the XRD test for 4 samples.

| Table 1. | Results | of sieving | analyses | for 12,626 | kg | Cilacap | iron | sand |
|----------|---------|------------|----------|------------|----|---------|------|------|
|----------|---------|------------|----------|------------|----|---------|------|------|

| Dortiolo oizo | | Weight of Sample code | | | | | | | | | | | |
|---------------|-------|-----------------------|-------|-------|-------|-------|-------|-------|--------|-------|--|--|--|
| (moch) | S1 | | S2 | 2 | Sa | 3 | S4 | 1 | TUL | 11 | | | |
| (mesn) - | g | % | g | % | g | % | g | % | g | % | | | |
| +40 | 197 | 6.24 | 154 | 5.21 | 170 | 5.38 | 147 | 4.39 | 668 | 5.29 | | | |
| -40+60 | 2,233 | 70.62 | 2,020 | 68.38 | 2,172 | 68.69 | 2,230 | 66.61 | 8,655 | 68.55 | | | |
| -60+80 | 635 | 20.08 | 685 | 23.19 | 721 | 22.80 | 855 | 25.54 | 2,896 | 22.94 | | | |
| -80 | 97 | 3.07 | 95 | 3.22 | 99 | 3.13 | 116 | 3.46 | 407 | 3.22 | | | |
| Total | 3,162 | 100 | 2,954 | 100 | 3,162 | 100 | 3,348 | 100 | 12,626 | 100 | | | |

Table 2. Chemical composition of Cilacap iron sand based on each fraction

| Particle Size | Chemi | cal Composition | (%) |
|---------------|----------|------------------|-------|
| (mesh) | Fe total | TiO ₂ | Wt. |
| +40 | 3.37 | 0.45 | 5.29 |
| -40+60 | 2.91 | 0.39 | 68.55 |
| -60+80 | 4.75 | 0.77 | 22.94 |
| -80 | 11.62 | 1.46 | 3.22 |

| Table 3 | Chemical | compositions | of magnetic se | naration | products |
|----------|----------|--------------|----------------|----------|----------|
| Table 5. | Chemical | compositions | or maynetic se | paradon | producis |

| | | Total iron | content within | TiO ₂ content within | | | | |
|-------------------|------|------------|----------------|---------------------------------|------|--------|--------|------|
| Magnetic Products | +40 | -40+60 | 60, 90 mach | -80 | +40 | -40+60 | -60+80 | -80 |
| | mesh | mesh | -00+00 mesn | mesh | mesh | mesh | mesh | mesh |
| 1000 G | 7.24 | 10.26 | 14.39 | - | 1.46 | 1.74 | 2.28 | - |
| 2000 G | 5.14 | 7.27 | 10.49 | - | 0.97 | 1.57 | 1.59 | - |
| 4000 G | 3.86 | 4.73 | 7.64 | - | 0.79 | 0.68 | 1.06 | - |
| Non-Mag | 1.96 | 2.22 | 3.47 | - | 0.44 | 0.25 | 0.57 | - |
| Original Sample | 3.37 | 2.91 | 4.75 | 11.62 | 0.45 | 0.39 | 0.77 | 1.46 |



Figure 3. XRD histogram for origin sample size -80 mesh







Figure 5. XRD histogram for 1000 G-magnetic product, size-60+80 mesh



Figure 6. XRD histogram for 1000 G-non-magnetic product, size-40+60 mesh

Table 2 presented relation among particle size, percent weight of each tested sizes and total iron of each fraction. The table showed that size 250 µm or 60 mesh was the dominant one retaining weight of 68.55% and the iron content of 54.85%. This implied that the iron mineral was dominantly distributed at minus 60 mesh while the highest iron content was available at minus 80 mesh performing the content of 11.62% but its percentage weight was only 3.22%. Figure 7 illustrated the particles size -60 mesh and -80 mesh. The former retained iron content of 2.91% while the later contained the iron of 11.62%. Based on its performance, the iron sand with -60 mesh was lighter in color than that of -80 mesh. The amount of silica content within the -60 mesh size was supposed to be the reason why such sands comprised light color.

Effect of particle size on the derived magnetic separation products was shown in Figure 8. Of the three magnetic intensities used in magnetic separation processes; it seemed that the higher the used magnetic intensity, the lesser the derived weights. A

particle with the size of -40+60 mesh that retained 68.55% provided the highest nonmagnetic products compared to other particle sizes. Yet for 4.000 G, the particles with a size of +40 mesh produced higher magnetic products than that of size -40+60and -60+80 meshes. A similar case occurred to other sizes, the 4.000 G gave magnetic products higher than that of 1.000 and 2.000 Gausses.

Referring to the analysis results for the distribution of total iron and titanium oxide, particle size and magnetic intensity; it is clear that the finer particle size the higher the quantities of both total iron and titanium oxide as shown in Figure 9. The figure also showed that the increase of total iron content was also followed by the increase of titanium oxide. The fact that the multiple increases of both materials were almost the same indicated that the iron and titanium minerals were still unified. The liberation degree between both minerals was still low. As a result, it was difficult to obtain magnetic products with high iron content but low TiO₂ matter in coarser particles.

| Table 4. | Particle | distribution | and iron | content of | Cilacap iron | sand |
|----------|----------|--------------|----------|------------|--------------|------|
| | | | | | | |

| Particle | Size | Weight | Total iron content | Distribution of total iron content | Cumulative weight of retained particles | Cumulative weight of total iron content |
|----------|------|--------|--------------------|------------------------------------|---|--|
| (mesh) | μm | % | % | % | % | % |
| +40 | 420 | 5.29 | 3.37 | 4.90 | 5.29 | 4.90 |
| -40+60 | 250 | 68.55 | 2.91 | 54.85 | 73.84 | 59.75 |
| -60+80 | 177 | 22.94 | 4.75 | 29.96 | 96.78 | 89.71 |
| -80 | ? | 3.22 | 11.62 | 10.29 | - | 100 |
| | | 100 | 3.637 | 100 | - | - |



Figure 7. Illustration of iron sand particle, size -60+80 and -80 meshes



Figure 8. Effect of particle size on the weight percent of magnetic separation products.



Figure 9. Effect of particle size on the recovered total iron and titanium oxide in magnetic separation.

The contents of both iron and titanium compositions in either original and product samples were the same. Both retained low contents. Geological condition affirmed that the samples came from the low-content iron deposit. Sunaryo and Sugihartono (2010) who analyzed titanomagnetite from iron sand using magnetic intensity of 1.3 Tesla, succeeded to increase the iron sand up to 82.25 wt% though the feed for magnetic separator came from different locations. Referring to such condition, the original samples needed to be examined in detail other valuable components. Commonly, the iron sand contained trace elements such as vanadium.

Based on XRF analysis (Table 5), vanadium pentoxide (V_2O_5) was detected within magnetic separation products. Such the products, included the magnetic product of (-60+80#. 1000 G) and the nonmagnetic one of (-40+60#, 4000 G), performed the contents of 0.089% and 0.011% respectively. The two products were selected to be reviewed their rare elements due to its high contents of their iron oxides (14.39%) and percent weight (77.2%). Yet the analysis also detected other rare element oxides namely strontium and gallium oxides. Sample with the code of -60+80 mesh/1000G/M showed SrO concentration of 0.033% while within the sample -40+60 mesh/4000G/NM, the SrO was 0.118%. It seemed that the amount of this element in the later sample (nonmagnetic products) was bigger than that of the former sample (magnetic product). Strontium oxide was normally used for cathode ray tubes to block X-ray emission. A similar condition also occurred to gallium oxide; the magnetic sample retained less concentration compared to non-magnetic ones. Commonly, the metal was employed for semiconductors, alloys and biomedical applications.

Of the four samples identified by XRD method, all samples showed similar contents, namely magnesium calcium aluminum iron silicate - $[Ca(Mg,Fe,Al)(Si,Al)_2O_6]$, magnetite - Fe_3O_4 , sodium calcium aluminum silicate - $(Ca,Na)(Si,Al)_4O_8$ (Table 6). All products contained magnetite, including the non-magnetic one.

 Table 5.
 Results of XRF analyses for magnetic and non-magnetic products of Cilacap iron sand after magnetic separation process.

| Sampla Cada | | Chemical Composition | | | | | | | | | | | | | | |
|--------------------------|------------------|----------------------|-----------|------|------|------|--------|----------|--------------------------------|------------------|-------|----------|-----------|-----------|-----------|-----------|
| Sample Code | SiO ₂ | TiO ₂ | AI_2O_3 | MnO | CaO | MgO | K_2O | P_2O_5 | Fe ₃ O ₄ | ZrO ₂ | SrO | V_2O_5 | Cr_2O_3 | Co_3O_4 | Ga_2O_3 | Sc_2O_3 |
| -60+80 mesh/ 1000G/M | 48.10 | 1.67 | 16.72 | 0.31 | 8.21 | 4.78 | 1.51 | 0.565 | 13.67 | 0.019 | 0.033 | 0.089 | 0.026 | 0.014 | 0.002 | 0.004 |
| -40+60 mesh/ 4000G/NM | 53.30 | 0.325 | 25.81 | 0.10 | 9.67 | 1.44 | 1.58 | 0.199 | 3.01 | 0.012 | 0.118 | 0.011 | 0.009 | 0.003 | 0.003 | 0.002 |

Table 6. Mineral composition available within magnetic separation products and original sample

| Sample code | Mineral composition | | | | | | |
|---|--|--|--|--|--|--|--|
| Original sample, -80 mesh | Magnesium calcium aluminum iron silicate, magnetite, sodium calcium aluminum silicate | [Ca(Mg,Fe,Al)(Si,Al) ₂ O ₆]; Fe ₃ O ₄ ; (Ca,Na)(Si,Al) ₄ O ₈ | | | | | |
| Non-magnetic product, - 40+60 mesh, 4000 G, NM | Magnesium calcium aluminum iron silicate, magnetite, sodium calcium aluminum silicate | [Ca(Mg,Fe,Al)(Si,Al) ₂ O ₆]; Fe ₃ O ₄ ; (Ca,Na)(Si,Al) ₄ O ₈ | | | | | |
| Magnetic product, -40+60 mesh, 1000 G, M | Magnesium calcium aluminum iron silicate, magnetite, sodium calcium aluminum silicate | [Ca(Mg,Fe,Al)(Si,Al) ₂ O ₆]; Fe ₃ O ₄ ; (Ca,Na)(Si,Al) ₄ O ₈ | | | | | |
| Magnetic product, -60+80 mesh 1000 G, M | Magnesium calcium aluminum iron silicate, magnetite, sodium calcium aluminum silicate | [Ca(Mg,Fe,Al)(Si,Al) ₂ O ₆]; Fe ₃ O ₄ ; (Ca,Na)(Si,Al) ₄ O ₈ | | | | | |

CONCLUSIONS

The particle size available within Cilacap iron sand mostly belonged to those that passed 40-mesh sieve. The obtained weight percentage from this sieve was 68.55% performing the total iron content of 2.91% and 1.74% TiO₂. The highest iron content was achieved at sieve of passing 80 mesh (11.62%) but its weight decreased to 3.22%.

The highest Fe and TiO₂ contents were achieved by the particle size of -40+60 mesh, namely 14.39% and 2.28% respectively. The recovery was 20.08%. Such a recovery was too low. Upgrading process required at least 59% Fe. However, this process has successfully increased the TiO₂ content more than 5 times, from 0.325 to 1.67%.

The results also showed some rare metal elements such as strontium (Sr), vanadium (V), cobalt (Co), gallium (Ga), and scandium (Sc) present with the degree of concentration that is guite interesting. This data could be a preliminary study to research further the rare metal elements in abundance deposit of iron sand. The rare metal elements are important components in the formation of advanced materials which their role and needs will continue to increase in the future.

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